

# **MODEL SOLUTIONS TO IIT JEE 2011**

## Paper II – Code 0

PART I							
1	2	3	4	5	6	7	8
С	D	B	Α	D	С	Α	В
9		10		11		12	
B, C, D		A, B, C, D		A, B, D		A, C, D	
	13	14	15	16	17	18	
	8	6	5	7	6	8	
-19				20			
A – r, s, t				A – p, r, s			
B – p, s				B – r, s			
C – r, s				C - t			
D – q, r				<b>D</b> – <b>p</b> , <b>q</b> , <b>r</b> , <b>t</b>			

6.

#### Section I

- 1.  $[Co(NH_3)_6]Cl_3$ ,  $Na_3[Co(ox)_3]$ ,  $[K_2Pt(CN)_4]$  &  $[Zn(H_2O)_6](NO_3)_2$  are diamagnetic.
- 2.  $E_{cell} = E_{cell}^{0} + \frac{0.06}{4} \log \frac{P_{O_2} \times [H^+]^4}{[Fe^{2+}]^2}$ = 1.67 + 0.015 log  $\frac{0.1 \times (10^{-3})^4}{(10^{-3})^2}$ = 1.67 - 0.015 × 7 = 1.57 V

3. RCH<sub>2</sub>OH H<sup>+</sup> OCH<sub>2</sub>R

- CuS & HgS are insoluble in dilute mineral acids. Cu<sup>2+</sup> & Hg<sup>2+</sup> ions belong to group II of qualitative analysis.
- 5. Haematite is  $Fe_2O_3$ . Oxidation state of Fe is +3 Magnetite is  $Fe_3O_4$ . Oxidation state of Fe is +2 and +3.

Aromatic primary amines form diazonium salt with NaNO<sub>2</sub> and HCl at low temperature which couples with  $\beta$ -naphthol to form coloured azo dye.

$$\Delta T_f = i \times K_f \times m$$
  
= 4 × 1.86 ×  $\frac{0.1}{329}$  × 10  
= 0.023  
F.P = -2.3 × 10<sup>-2</sup> °C

8. The structure given is that of  $\beta$ –D–glucose.

#### Section II

- Cu<sup>+2</sup> is reduced to Cu<sup>+1</sup> by CN<sup>-</sup> & SCN<sup>-</sup> CuCl<sub>2</sub> in aqueous acidic medium is reduced to CuCl on boiling with metallic Cu
- In (B), (C) and (D), X–(CH<sub>2</sub>)<sub>4</sub>–X is converted to a diamine which can form condensation polymer with adipic acid. In (A), X–(CH<sub>2</sub>)<sub>4</sub>–X is converted to a diol which gives polyester.

11. K = 
$$\frac{0.693}{t_{1/2}}$$

K increases with increase of temperature and hence half life decreases.

$$t = \frac{\frac{t_{1/2}}{0.3} \log \frac{100}{0.4}}{0.4} = \frac{8t_{1/2}}{2}$$
  
R = R\_0 e^{-kt}

12.  $MnO_4^- \rightarrow Mn^{2+}$  (acid medium)  $MnO_4^- \rightarrow MnO_2$  (Neutral and aqueous mediums)

#### Section III

- 13. A truncated octahedrous has 8 hexagonal and 6 square faces. (36 edges and 24 vertices)
- 14. There are six C H bonds that can involve in hyperconjugation.
- 15.  $PCI_5 + SO_2 \rightarrow POCI_3 + SOCI_2$   $PCI_5 + H_2O \rightarrow POCI_3 + 2HCI$   $PCI_5 + H_2SO_4 \rightarrow SO_2CI_2 + 2POCI_3 + 2HCI$   $6PCI_5 + P_4O_{10} \rightarrow 10POCI_3$  $PCI_5 \rightarrow PCI_3 + CI_2, 2PCI_3 + O_2 \rightarrow 2POCI_3$
- 16. [Cl<sup>¬</sup>] from CuCl = 10<sup>-3</sup>  $K_{sp}(AgCl) = [Ag^+] [Cl<sup>¬</sup>]$  $[Ag^+] = \frac{1.6 \times 10^{-10}}{10^{-3}} = 1.6 \times 10^{-7}$
- 17. Millimoles of  $CI^{-} = 30 \times 0.01 \times 2$ = 0.6 Vol. of 0.1 M AgNO<sub>3</sub> =  $\frac{0.6}{0.1}$  = 6 mL



- 19. (A) is intramolecular aldol condensation
  - (B) involves Grignard reagent addition to carbonyl compound.
  - (C) involves nucleophilic addition and dehydration.
  - (D) involves dehydration and intramolecular Friedel–Craft reaction.
- 20. (A) involves transition from solid to gas phase with the absorption of heat.
  - (B) is exothermic and a gaseous product is formed from a solid.
  - (C) involves association
  - (D) white phosphorous is converted to the polymeric red allotropic form on heating. Different solids are considered as different phases.



#### PART II

27. If non-conservative induced electric field this

$$\begin{array}{c} R \\ \hline Z_{B} \end{array} X_{C}^{B} \\ X_{C}^{B} = \frac{1}{C\omega} < X_{C}^{A} \\ \Rightarrow Z_{B} < Z_{A} \\ \Rightarrow I_{R}^{B} > I_{R}^{A} \text{ and } V_{C}^{A} > V_{C}^{B} \end{array}$$

- 30. During collision, an impulse is exerted on the ring which has a horizontal component (towards right) and a vertical component (downwards). This produces an additional upward normal reaction (by floor on ring) and a horizontal frictional force (towards left)  $\Rightarrow$  (C) is correct. Since kinetic frictional force is not a finite force (due to varying N) acting for an infinitesimally small duration, its effect on changing the momentum of ring during collision is not negligible. Hence, conservation of horizontal linear momentum cannot be applied.
- 31. +q1 -+q2  $(or - q_1) = 0$  $(-q_2)$

$$\begin{split} W_{agent} &= \Delta U = q(V_2 - V_1) \\ &= 1 \times (V_B - V_A) \\ &= (V_B - V_A) \end{split}$$

32.  $Vd_A + Vd_B = 2Vd_F = 0$  $\therefore$  d<sub>A</sub> + d<sub>B</sub> = 2d<sub>F</sub> Obviously  $d_A < d_F$  and  $d_B > d_F$ 

#### Section III

- 33.  $\frac{\frac{4}{3}}{v} \frac{1}{-24} = \frac{\frac{7}{4} 1}{6} + \frac{\frac{4}{3} \frac{7}{4}}{\infty}$  $\Rightarrow$  v = 16 from top surface of liquid  $\Rightarrow$  2 cm from bottom surface of liquid
- 34.  $h\upsilon = \frac{1242 \text{ eV nm}}{200 \text{ nm}} = 6.21 \text{ eV}$ KE = 6.21 - 4.7 = 1.51 eV
  - $\frac{kq}{r} = 1.5$  V for stopping electrons.

$$\therefore q = \frac{1.5 \times (10^{-2})}{9 \times 10^9} = Ne$$
$$\therefore N = 1 \times 10^7$$

35.  $T = \frac{2u\sin 60^{\circ}}{g} = \frac{2 \times 10 \times \sqrt{3}}{10 \times 2} = \sqrt{3} s$  $(u \cos\theta) T = \frac{1}{2} aT^2 + 1.15$  $(u = 10 \text{ m s}^{-1})$  $\Rightarrow a = 5 \text{ m s}^{-2}$ 

36. 
$$E_{eff} = \frac{E_1 r_2 + E_2 r_1}{(r_1 + r_2)}$$
$$= \frac{(6 \times 2) + (1 \times 3)}{(1 + 2)}$$
$$= 5 V$$

37. 
$$\frac{1}{2} \text{mv}^2 = \mu \text{mg S} + \frac{1}{2} \text{kS}^2$$
  
m = 0.18 kg,  $\mu = 0.1$ ,  
g = 10 m s<sup>-2</sup>, S = 0.06 m  
 $\Rightarrow v^2 = 0.12 + 0.04 = 0.16$   
 $\Rightarrow v = \sqrt{0.16} = 0.4 \text{ m s}^{-1}$   
 $= \frac{4}{10} \Rightarrow \text{N} = 4$ 

38. 
$$Z^{2} = R^{2} + X_{C}^{2}$$
$$\Rightarrow X_{C}^{2} = 1.25 R^{2} - R^{2}$$
$$= 0.25 R^{2}$$
$$\Rightarrow X_{C} = 0.5 R$$
$$\Rightarrow C = \frac{1}{X_{C}\omega} = \frac{1}{0.5 R \times 500} = \frac{1}{250 R}$$
$$\tau = RC = \frac{1}{250} s = 4 ms$$
Section IV

#### Section IV

- 39. Knowledge based.
- 40. Knowledge based.

#### PART III

41 42 44 45 43 46 47 48 B D Α A B С D С 49 50 51 52 A, D Α **A**, **B**, **D** A, B, C, D 53 54 55 56 57 58 3\* 2 9 2 0 9 59 60 A - sA - q $\mathbf{B} - \mathbf{t}$ B - p/p, q, r, s, tC – r C - sD – r **D** – t\* Section I  $= fog(sin(x)^{2})$  $= f(sin(sin(x^2)))$  $= \sin^2(\sin(x^2))$ 41. Let  $\alpha$  denote the common root  $gogof(x) = gog(x^2)$  $\alpha^2 + b\alpha - 1 = 0$  $= g(sin(x)^2)$  $\alpha^2 + \alpha + b = 0$  $= sin(sin (x^2))$  $b\alpha - 1 = \alpha + b$  $\therefore \sin^2(\sin(x^2) = \sin \sin(x^2))$  $\alpha$  (b – 1) = b + 1  $\Rightarrow$  sin(sin(x<sup>2</sup>) (sin sin(x<sup>2</sup>) -1) = 0  $\alpha = \frac{b+1}{b-1}$  $\Rightarrow$  sin(sin(x<sup>2</sup>) = 0 or sin (sin(x<sup>2</sup>) = 1  $\Rightarrow$  sin(x<sup>2</sup>) = 0 sin (x<sup>2</sup>)  $(b + 1)^{2} + b(b^{2} - 1) - (b - 1)^{2} = 0$  $\Rightarrow x^2 = n\pi$  $4b + b(b^2 - 1) = 0$  $\therefore x = \pm \sqrt{n\pi} \quad n = \{0, 1, 2 \dots \}$  $4 + b^2 = 0$  $b^2 = -3$  $b = i\sqrt{3}$ a b 44. for non-singular matrics,  $|\omega| = 1 |c| \neq 0$ <sub>0</sub>π<sup>2</sup> 42. Let the circle be 1 ω  $x^{2} + y^{2} + 2gx + 2fy + c =$  $\Rightarrow$  1 - c $\omega$  - a $\omega$  - ac $\omega^2 \neq$  0 Passed thro  $(-1, 0) \longrightarrow -2g + c = -1(1)$  $(1 - a\omega) (1 - c\omega) \neq 0$ Passes thro  $(0, 2) \longrightarrow 4f + c =$ →(2)  $\Rightarrow$  a  $\neq \frac{1}{\omega} = \omega^2$  and c  $\neq \frac{1}{\omega} = \omega^2$  $\sqrt{g^2 + f^2} - c = g$  $f^2 - c = 0$  $\therefore$  a = c =  $\omega$  and b =  $\omega$  pr  $\omega^2$ Hence there are two such matrices.  $4f + f^2 = -4$ 45. Let the point be ' $\theta$ '  $(f+2)^2 = 0 \Longrightarrow f = -2$ Normal at  $\theta$  is  $\Rightarrow$  c = -4 - 4f = 4 $\frac{ax}{\sec\theta} + \frac{by}{\tan\theta} = a^2 + b^2$  $2g = 5, g = \frac{5}{2}$ Normal passes thro (9, 0) Circles is  $x^2 + y^2 + 5x - 4y + 4 = 0$  $\frac{9a}{a} = a^2 + b^2$  (1) (-4, 0) satisfies the equation sec θ a sec  $\theta = 6$ 43. fogogo f(x)

 $= fogog(x^2)$ 

 $f^2 = c$ 

$$\sec \theta = \frac{6}{a}$$
(1) reduces
$$9 a \times \frac{a}{6} = a^{2} + b^{2}$$

$$\frac{3a^{2}}{2} = a^{2} + b^{2}$$

$$= a^{2} + a^{2} (e^{2} - 1)$$

$$\frac{3}{2} = 1 + e^{2} - 1$$

$$= e^{2}$$

$$e = \sqrt{\frac{3}{2}}$$

46.

$$f(x) = f(1 - x)$$

$$\Rightarrow \text{ curve is symmetrical about } x = \frac{1}{2}$$

$$R_{1} = \int_{1}^{2} xf(x) dx$$

$$= \int_{1}^{2} (-1 + 2 - x) f(-1 + 2 - x) dx$$

$$\int_{1}^{2} (1 - x) f(1 - x) dx$$

$$= \int_{-1}^{2} (1 - x) f(x) dx$$

$$= \int_{-1}^{2} f(x) dx - \int_{-1}^{2} xf(x) dx$$

$$= R_{2} - R_{1}$$

$$2R_{1} = R_{2}$$

$$(1 - x) f(x) dx$$

47. Which is of the form  $1^{\alpha}$   $\lim_{e^{x\to 0}} (f(x)-1)g(x)$ 

$$= e^{(1+x \log(1+b^2)-1)\frac{1}{x}}$$
$$= e^{\frac{x \log(1+b^2)}{x}}$$
$$= e^{\log(1+b^2)}$$
$$\therefore 1 + b^2 = 2b \sin^2\theta$$
$$\sin^2\theta = \frac{1+b^2}{2b}$$

Since 
$$b > 0$$
  
 $\therefore \theta = \pm \frac{\pi}{2}$   
48.  

$$A = \frac{1}{2}$$

$$A = \frac{1}{2}$$

$$B = \frac{1}{3}$$
Let P be (x, y)  
 $X = \frac{t^2}{4}, Y = \frac{2t}{4}$ 
Lows of P is  
 $4X = 4Y^2$   
 $\Rightarrow Y^2 = X$ 

### Section II

49. 
$$P(E \cap \overline{F}) + P(F \cap \overline{E}) = \frac{11}{25}$$
Also 
$$P(\overline{E} \cap \overline{F}) = \frac{2}{25}$$
But 
$$P(E \cap \overline{F}) = P(E \cap \overline{F}) = P(\overline{E \cup F})$$

$$\therefore P(E \cap F) = 1 - \frac{2}{25} = \frac{23}{25}$$

$$P(E \cup F) = 1 - \frac{2}{25} = \frac{23}{25}$$

$$P(E \cup F) = P(E \cap \overline{F}) + P(F \cap \overline{E}) + P(E \cap F)$$
(refer figure)
$$\therefore \frac{23}{25} = \frac{11}{25} + P(E \cap F)$$

$$\therefore P(E \cap F) = \frac{12}{25} = P(E) \times P(F)$$
From the options
$$P(E) = \frac{3}{5} \text{ and } P(F) = \frac{4}{5}$$
or
$$P(E) = \frac{4}{5} \text{ and } P(F) = \frac{3}{5}$$

- 50.  $f(x) = \frac{b x}{1 bx}$ f: (0, 1)  $\rightarrow$  R In the given range f(x) is not on to, and hence f<sup>1</sup>(x) does not exist.
- 51. Normal at 't' is  $y + xt = 2t + t^3$

 $6 + 9t = 2t + t^{3}$   $t^{3} - 7t - 6 = 0$  t = -1, t = -2, t = 3Normal are y - x = -3,And y + 3x = 33And y - 2x = -12

52. 
$$f\left(-\frac{\pi}{2}\right) = 0$$
$$f\left(\frac{-\pi}{2}\right) = -\cos\left(\frac{-\pi}{2}\right) = 0$$

(A) is true f(x) is continuous at x = 0 f'(0<sup>-</sup>) = 0 f'(0<sup>+</sup>) = 1 (B) is true F(x) is continuous at x = 1 f'(1<sup>-</sup>) = 1 f'(1<sup>+</sup>) = 1 f(x) is differentiable at x = 1. (c) is true.  $\frac{22}{14} = \frac{11}{7} = 1$   $x = \frac{-3}{2} \text{ lies in } \left(-\infty, \frac{-\pi}{2}\right)$ 

 $\Rightarrow$  f(x) is differentiable there, since f(x) is a linear function in that interval (D) is true.

#### Section III

53. 
$$M = \begin{pmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{pmatrix}$$
$$M \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} = \begin{pmatrix} -1 \\ 2 \\ 3 \end{pmatrix} \Rightarrow a_2 = -1; b_2 = 2; c_2 = 3$$
$$M \begin{pmatrix} 1 \\ -1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix} \Rightarrow a_1 + 1 = 1 \Rightarrow a_1 = 0$$
$$C_1 - 3 = -1 \Rightarrow c_1 = 2$$
$$M = \begin{pmatrix} 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 12 \end{pmatrix} \Rightarrow 2 + 3 + c_3 = 12$$
$$\Rightarrow c_3 = 7.$$
$$A_1 + b_2 + c_3 = 0 + 2 + 7 = 9$$



All points  $\in$  S lies inside the circle, except  $\left(\frac{5}{2}, \frac{3}{4}\right)$  and  $\left(\frac{1}{8}, \frac{1}{4}\right)$  satisfies the inequality

2x - 3y - 1 < 0.  $\therefore$  The remaining 2 points lie on the smaller intersection.

55. \*Assuming 
$$\omega = e^{\frac{i2\pi}{3}}$$
  
 $1 + \omega + \omega^2 = 0$   
 $|x|^2 + |y|^2 + |z|^2$   
 $= (a + b + c) (\overline{a} + \overline{b} + \overline{c})$   
 $+ (a + b\omega + c\omega^2)(\overline{a} + \overline{b}\omega^2 + \overline{c}\omega)$   
 $+ (a + b\omega^2 + c\omega)(\overline{a} + \overline{b}\omega + \overline{c}\omega^2)$   
 $= 3(|a|^2 + |b|^2 + |c|^2)$   
 $\therefore \frac{|x|^2 + |y|^2 + |z|^2}{|a|^2 + |b|^2 + |c|^2} = 3$ 

56. I. 
$$F = e^{g(x)}$$

... Differential Equation is  $ye^{g(x)} = g(x) g'(x) e^{g(x)}$ Let g(x) = t $ye^{t} = \int te^{t} dt$ 

$$ye^{t} = \int te^{t} dt$$
  
 $ye^{t} = te^{t} - \int 1.e^{t} dt$ 

 $= te^{t} - e^{t} + c$ = (t - 1) e<sup>t</sup> + c  $\therefore y = (t - 1) + c e^{-t}$  $\therefore y(x) = (g(x) - 1) + c e^{-g(x)}$  $x = 0 \Longrightarrow y = 0$  $\therefore c = 1$  $y(x) = (g(x) - 1) + e^{-g(x)}$  $\therefore y(2) = (g(2) - 1 + e^{-g(2)})$ = 0 - 1 + 1 = 0

57. 
$$x^4 - 4x^3 + 12x^2 + x - 1 = 0$$
  
 $f(0) < 0, f(1) > 0$   
∴ one root in (0, 1)  
 $f^1(x) = 4x^3 - 12x^2 + 24x + 1$   
 $f^{11}(x) = 12(x^2 - 2x + 2) > 0$ 

0

$$\Rightarrow f^{1}(x) \text{ is increasing}$$
  

$$\therefore \text{ it has exactly one root}$$
  

$$\Rightarrow f(x) \text{ may have almost 2 distinct roots}$$
  
Since real roots are even in number  

$$f(x) \text{ has 2 distinct real roots}$$

58. 
$$(\overline{r} - \overline{c}) \times \overline{b} = 0$$
  
 $\overline{r} = \overline{c} + m \overline{b}$   
 $0 = \overline{r} \cdot \overline{a} = \overline{c} \cdot \overline{a} + \overline{m} \overline{b} \cdot \overline{a}$   
 $= -4 + m, \quad m = 4$   
 $\overline{r} = \overline{c} + 4\overline{b}$   
 $\overline{r} \cdot \overline{b} = \overline{c} \cdot \overline{b} + 4\overline{b}^2$   
 $= 1 + 8 = 9$   
 $\in (-\infty, -1] \cup [1, \infty)$ 

# Section IV

59. (a) 
$$R_e\left(\frac{2iz}{1-z^2}\right)$$
  
 $R_e\left[\frac{2i}{\frac{1}{z}-z}\right]$   
 $= R_e\left(\frac{2i}{\overline{z}-z}\right)$   
 $= R_e\left(\frac{2i}{\overline{z}-z}\right)$   
 $= R_e\left(\frac{1}{(-\operatorname{Im} z)}\right)$   
 $= \frac{1}{-\operatorname{Im} z}$   
(b) Put  $y = 3^{x-1}$   
 $-1\frac{<\frac{8}{3}y}{1-y^2} \le 1$   
 $\Rightarrow \left|\frac{8}{3}xy\right| \le \left|1-xy^2\right|$   
 $\Rightarrow \frac{8}{3}y \le 1-y^2$  if  $1-y^2 \ge 0$   
 $3y^2 \cdot 8y - 3 \le 0$  if  $y^c = [-1, 1]$ 

$$\Rightarrow \frac{5}{3} y \le 1 - y^2 \qquad \text{if } 1 - y^2 \ge 0$$
  

$$3y^2 + 8y - 3 \le 0 \qquad \text{i.e } y^{\epsilon} [-1, 1]$$
  

$$3y^2 + 8y - y - 3 \le 0$$
  

$$(3y - 1) (y + 3) \le 0 \quad y \in \left[-3, \frac{1}{3}\right]$$
  

$$y \in \left[0, \frac{1}{3}\right] = 3^{-1} \le \frac{1}{3}$$
  

$$x \le 0$$
  

$$\frac{8}{3} y \le y^2 - 1 \quad \text{if } 1 - y^2 \le 0$$
  

$$3y^2 - 8y - 3 \ge 0$$
  

$$3y^2 - 9y + y - 3 \ge 0$$
  

$$(3y + 1) (y - 3) \ge 0 \qquad y \ge 3$$
  

$$\Rightarrow 3^{x - 1} \ge 3$$

$$x \ge 2 \quad (r, t)$$
  

$$\therefore x \in (-\infty, 0] \cup [z, \infty)$$
(c) 
$$\frac{1}{\cos^{3}\theta} \begin{vmatrix} \cos\theta & \sin\theta & \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta & \sin\theta \\ -\cos\theta & -\sin\theta & \cos\theta \end{vmatrix}$$

$$= \frac{1}{\cos^{3}\theta} \begin{vmatrix} 0 & 0 & 2\cos\theta \\ -\sin\theta & \cos\theta & \sin\theta \\ -\cos\theta & -\sin\theta & \cos\theta \end{vmatrix}$$

$$= \frac{2\cos\theta}{\cos^{3}\theta} = 2\sec^{2}\theta \in [2,\infty)$$
(d) 
$$\frac{x^{2}}{2}(3x-10)$$

$$= \frac{5}{3x^{2}}-10x^{2}$$

$$f'(x) = \frac{15}{2}x^{\frac{3}{2}}-15\sqrt{x}$$

$$= 15\sqrt{x}(\frac{x}{2}-1) \ge 0$$
If  $x \ge 2$ .  
60. (a)  $\cos\theta = \frac{-1+3}{4} = \frac{1}{2}$   

$$\therefore \text{ required angle is } \pi - \frac{\pi}{3} = \frac{2\pi}{3}$$
(b) 
$$\int_{a}^{x} (f(x)-3x)dx = a^{2}-x^{2}$$

$$f(x) - 3x = -2x \Rightarrow f(x) = x$$

$$\therefore f\left(\frac{\pi}{6}\right) = \frac{\pi}{6}$$
Let  $f(x) = \frac{a+b}{2}$  (independent of x). This satisfies the given equation. So we can always set the values of a and b such that  $f\left(\frac{\pi}{6}\right) = \frac{\pi}{6}, \frac{2\pi}{3}, \frac{\pi}{3}, \pi \text{ or } \frac{\pi}{2}$ .  
(c)  $\frac{\pi}{\log 3} \log[\sec \pi x + \tan \pi x]\frac{56}{76} = \pi$ 
(d) 
$$|\operatorname{Arg}\left(\frac{1}{z-1}\right)| = |\operatorname{Arg}(z-1)|$$
Maximum value  $= \frac{\pi}{2}$ , but it is never attained\*.